# An Improved Implementation of Effective Number of Codons $(N_c)$

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#### Abstract

The effective number of codons ( $N_c$ ) is a widely used index for characterizing codon usage bias because it does not require a set of reference genes as does codon adaptation index (CAI) and because of the freely available computational tools such as CodonW. However,  $N_c$  as originally formulated has many problems. For example, it can have values far greater than the number of sense codons; it treats a 6-fold compound codon family as a single-codon family although it is made of a 2-fold and a 4-fold codon family that can be under dramatically different selection for codon usage bias; the existing implementations do not handle all different genetic codes; it is often biased by codon families with a small number of codons. We developed a new  $N_c$  that has a number of advantages over the original  $N_c$ . Its maximum value equals the number of sense codons when all synonymous codons are used equally, and its minimum value equals the number of codon families when exactly one codon families with a synonymous codon families (e.g., those involving amino acids coded by six synonymous codons) into 2-fold and 4-fold codon families. It reduces the effect of codon families with few codons by introducing pseudocount and weighted averages. The new  $N_c$  has significantly improved correlation with CAI than the original  $N_c$  from CodonW based on protein-coding genes from *Saccharomyces cerevisiae, Caenorhabditis elegans, Drosophila melanogaster, Escherichia coli, Bacillus subtilis, Micrococcus luteus,* and *Mycoplasma genitalium.* It also correlates better with protein abundance data from the yeast than the original  $N_c$ .

Key words: effective number of codons, codon usage, codon adaptation, translation elongation, gene expression.

### Introduction

Ever since the empirical documentation of the correlation between codon usage and transfer RNA (tRNA) abundance (Ikemura 1981), studies on codon-anticodon adaptation have progressed in theoretical elaboration (Bulmer 1987, 1991; Xia 1998, 2008; Higgs and Ran 2008; Jia and Higgs 2008; Palidwor et al. 2010), in critical tests of alternative theoretical predictions (Xia 1996, 2005; Carullo and Xia 2008; van Weringh et al. 2011), and, in particular, in formulation and improvement of various codon usage indices to characterize codon usage bias (Sharp and Li 1987; Wright 1990; Xia 2007). Codon usage indices such as CAI (Sharp and Li 1987; Xia 2007) are positively correlated not only with translation elongation efficiency but also with splicing strength of yeast intron splice sites (Ma and Xia 2011) and translation initiation efficiency measured by ribosomal loading (Xia et al. 2011).

Codon usage bias is often measured by two classes of indices, one class being codon specific and the other being gene specific. A representative of the first class is the relative synonymous codon usage (Sharp et al. 1986), and representatives of the second class are the effective number of codons or  $N_c$  (Wright 1990), the Codon Adaptation Index (CAI; Sharp and Li 1987; Xia 2007), the frequency of optimal codons or  $F_{op}$  (Ikemura 1981), and the codon bias index (CBI; Bennetzen and Hall 1982). Although comparative studies (Comeron and Aguade 1998; Duret and Mouchiroud 1999; Coghlan and Wolfe 2000) suggest that CAI is the best in predicting gene expression levels, N<sub>c</sub> has one advantage over CAI, F<sub>op</sub>, or CBI in that it does not require external information (which is often unavailable) other than the codon frequencies of the gene. In contrast, CAI requires a reference set of known highly expressed genes, Fop needs information on relative tRNA abundance (it defines translationally optimal codons as those forming Watson-Crick base pair with the anticodon of major tRNA species in each codon family), and CBI needs information on both gene expression and relative tRNA abundance. For this reason,  $N_c$  has been frequently used in biological research to characterize codon usage bias, partly facilitated by the CodonW program and its web server at http://mobyle.pasteur.fr/cgi-bin/portal.py#forms::codonw (last accessed August 28, 2012).

Sometimes additional information on tRNA does not help predict gene expression or codon usage. For example, the *Bacillus subtilis* genome codes a tRNA<sup>Ala/GGC</sup> for decoding GCY codons. The GCC codon, which forms Watson–Crick base pair with the anticodon, is not used as frequently as the GCU codon which wobble-pairs with the anticodon. One might argue that, according to previous studies

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(Grosjean et al. 1978; Fiers and Grosjean 1979; Grantham et al. 1981; Ikemura 1981), the intermediate binding strength between codon and anticodon is optimal, especially for highly expressed genes. A weak binding at the third codon position is preferred with strong binding at the first two codon positions, and a strong binding at the first two codon positions. Thus, GCU is preferred because of the strong binding in the first two positions. However, this explanation does not work for Gly where four tRNA<sup>Gly/GCC</sup> genes are present for decoding GGY codons, and GGC is used more frequently than GGU. Before we gain a better understanding between codon–anticodon adaptation, codon usage bias indices, such as  $N_{cr}$  remain useful.

However, there are several problems with  $N_{c}$  both in concept and in computer implementation, that affect its performance and limit its application. We will detail them individually and propose modifications and improvements.

#### Conceptual Problems with $N_c$ and Solutions

To facilitate presentation, we will list the  $N_c$ -related definitions below. For an individual codon family of m synonymous codons whose counts are  $n_1, n_2, \ldots, n_m$ , we have  $n = \sum n_i$  and  $p_i = n_i/n$ . The original  $N_c$  formulation for this codon family is as follows:

$$F_{CF} = \frac{n \sum_{i=1}^{m} p_i^2 - 1}{n - 1}$$
(1)  
$$N_{c,CF} = 1/F_{CF}$$

where the subscript CF stands for "codon family" and refers to the fact that  $F_{CF}$  and  $N_{cCF}$  are for a specific codon family instead of for a gene.

One problem, which was recognized at the very beginning (Wright 1990), is that  $N_{cCF}$  can have values much greater than m. For example, if a 4-fold GGN codon family (m = 4) has  $n_i$  = 2, then n = 8,  $p_i$  = 0.25, and  $N_{c,CE}$  = 7 according to equation (1) instead of the maximum expected value of 4. When  $N_{\rm c.CF}$  values from different codon families are compiled to arrive at a final  $N_c$  value for a gene, the value can be much greater than 61 for a standard genetic code, especially when n is small. This problem has not been fixed except by a post hoc rescaling of the resulting  $N_c$  values, such as is done in CodonW (e.g., the  $N_c$  values are rescaled to the range of 20–61 for standard genetic code). Such rescaling does not address the problem that  $N_c$  for a gene can be dramatically biased by codon families each with few codons. In addition, the rescaling is conceptually confusing. For example, when one obtains an  $N_c$  of 61, one expects the codon usage to be equal (unbiased). However, almost all genes with an  $N_c$  value of 61 computed from CodonW actually do not use synonymous codons equally. In other words, many genes get an  $N_c$  value of 61 for wrong reasons. It is paradoxical that the formulation of  $F_{CF}$  in equation (1), originally intended for correcting bias associated with small n in measuring homozygosity in population genetics, becomes the very source of often dramatic

bias associated with small n in the context of measuring codon usage bias.

Another problem with the formulation in equation (1) is the loss of information. If n = 2 for a 2-fold codon family with  $n_1 = n_2 = 1$ , then  $F_{CF}$  is 0, and the data cannot be used to compute  $N_{c.CF}$ . For a 3-fold codon family,  $F_{CF}$  is also 0 when  $n_1 = n_2 = n_3 = 1$  or when  $n_1 = n_2 = 1$  and  $n_3 = 0$ . For a 4-fold codon family,  $F_{CF}$  is also 0 when  $n_1 = n_2 = n_3 = n_4 = 1$  or when  $n_1 = n_2 = n_3 = 1$  and  $n_4 = 0$ . This implies that information contained in codon families with a small n often cannot be used.

To alleviate the two problems above, one may redefine *F* simply as

$$F_{\rm CF} = \sum_{i=1}^{m} p_i^2 \tag{2}$$

Now the maximum  $N_c$  for a codon family with *m* codons will be exactly *m* (when synonymous codons are equally used), so that, for the standard genetic code, the maximum possible value for  $N_c$  would be exactly 61. The minimum of  $N_c$  based on  $F_{CF}$  in equation (2) is the number of codon families when only one codon is used in each codon family.  $F_{CF}$  in equation (2) and that in equation (1) approach each other when *n* becomes very large. When *n* is small,  $F_{CF}$  in equation (2) is more preferable than that in equation (1). As will be shown later, the new  $F_{CF}$  not only eliminates the clumsy need for  $N_c$  rescaling but also leads to better prediction of protein abundance and better correlation with CAI.

We have not yet addressed the potential bias introduced by small *n*. Suppose we have a 2-fold codon family with  $n_1 = 90$  and  $n_2 = 10$ . This would give us an  $N_{c,CF}$  of 1.22 based on  $F_{CF}$  defined in equation (2). However, if we have  $n_1 = 9$  and  $n_2 = 1$ , the resulting  $N_{c,CF}$  is the same, but  $N_{c,CF}$  with n = 100 is clearly more trustworthy than  $N_{c,CF}$  with n = 10. Proper handling of small *n* values is crucial for a good codon usage index.

Two commonly used approaches to alleviate the effect of a small n are 1) pseudocount and 2) weighting. With the pseudocount approach, we may redefine

$$F_{\rm CF} = \sum_{i=1}^{m} \left(\frac{n_i+1}{n+m}\right)^2 \tag{3}$$

Equation (3) implies that, when there is no information for a codon family (i.e., when n = 0), then we assume equal codon usage. This is reasonable biologically because a codon family that is hardly used is expected not to be under strong selection for codon usage bias, although mutation bias may also cause codon usage bias (Xia 1996, 2005). The approach is also reasonable statistically because we adopt the (implicit) null hypothesis of no codon usage bias when there is no data to reject it. A more general specification of the pseudocount approach is to replace 1 in the numerator of equation (3) by a constant *C* and the *m* in the denominator by  $m^*C$ . In conjunction with the pseudocount approach, we may also specify a minimum *n* for a codon family to be included in computing  $N_c$ .

Although the pseudocount approach can be applied to the computation of  $F_{CF}$ , the weighting approach can

be applied to compiling individual  $N_{c,CF}$  values to the final  $N_c$  value for the gene so as to minimize the potential bias introduced by codon families with small n values. Suppose we have three 2-fold codon families, with  $n_1 = n_2 = 200$ ,  $n_3 = 4$ , and  $F_{CF1} = F_{CF2} = 1$ , and  $F_{CF3} = 0.5$ . The average of the three F values ( $\bar{F}$ ) is 2.5/3  $\approx$  0.8333, and the number of effective codons contributed by the three codon families is  $3/\bar{F} = 3.6$ . However, it is unreasonable to have equal weight for the three F values obtained with dramatically different n values. A weighted  $\bar{F}$  is

$$\bar{F} = \frac{n_1 F_{\text{CF1}} + n_2 F_{\text{CF2}} + n_3 F_{\text{CF3}}}{n_1 + n_2 + n_3} = \frac{402}{404} \approx 0.9951 \quad (4)$$

Thus, the three codon families will contribute only 3.0149  $(=3/\overline{F})$  to the final  $N_c$  instead of 3.6 as before. Such a value reflects better the extremely strong codon usage bias observed in the two codon families with a large n, which suggests strong codon usage bias.

With the weighting scheme, the final gene-specific  $N_c$  is

$$N_{\rm c} = N_{\rm s} + \frac{K_2 \sum_{j}^{K_2} n_j}{\sum_{j=1}^{K_2} (n_j F_{\rm CF,j})} + \frac{K_3 \sum_{j}^{K_3} n_j}{\sum_{j=1}^{K_3} (n_j F_{\rm CF,j})} + \frac{K_4 \sum_{j}^{K_4} n_j}{\sum_{j=1}^{K_4} (n_j F_{\rm CF,j})}$$
(5)

where  $N_s$  is the number of codon families with a single codon, for example, the Met and the Trp codon families in the standard genetic code, with a single AUG and UGG codon, respectively,  $F_{CE,i}$  is  $F_{CE}$ , defined in equation (3) for codon family *j*, and  $K_i$  is the number of *i*-fold codon families. There are cases where  $N_s \neq 2$ . For example, the vertebrate mitochondrial code (transl table = 2) has  $N_s = 0$ . In contrast, the alternative yeast nuclear code (transl\_table = 12) has  $N_s$  equal to 3, that is, with a Ser family containing a single CUG codon in addition to the Met and Trp codon families. Similarly, Blepharisma nuclear code (transl table = 15) has an additional singlecodon Gln (UGA) codon family, leading to  $N_s = 3$ . Two other genetic codes with  $N_s = 3$  are the Chlorophycean mitochondrial code (transl table = 16) and the Scenedesmus obliquus mitochondrial code (transl\_table = 22), each with an single-codon Leu (UAG) codon additional family. Thraustochytrium mitochondrial code (transl\_table = 23) also has  $N_s = 3$  with an additional single-codon Leu (UUG) codon family.

Most of the known genetic code have only one 3-fold codon family, that is, the lle codon family, so  $K_3 = 1$ . However, there are several exceptions. For example, in addition to the 3-fold lle codon family, the echinoderm and flatworm mitochondrial code (transl\_table = 9) has a 3-fold Asn (AAH, where H stands for A, C, or U) codon family, the euplotid nuclear code (transl\_table = 10) has a 3-fold Cys (UGH) codon family, and the alternative yeast nuclear code (transl\_table = 12) has a 3-fold Leu (CUH) codon family. In particular, the alternative flatworm mitochondrial code (transl\_table = 14) has three 3-fold codon families, lle (AUH), Asn (AAH), and Tyr (UAH). Multiple 3-fold codon families in one genetic code were unknown to Wright when he formulated  $N_c$  (Wright 1990). Equation (5) does not include 6-fold or 8-fold compound codon families. We provide reasons for why such compound codon families should be broken into two separate codon families in computing  $N_c$  in the next section.

#### Implementation Problems with $N_c$ and Solutions

There are two problems with the implementation of  $N_c$ . The first involves the diverse array of genetic codes. Few implementations of  $N_c$  accommodate all genetic codes, which have now numbered 18. Currently, the most comprehensive  $N_c$  implementation is CodonW, which accommodates eight different genetic codes. However, there is a misspecification of the yeast mitochondrial code. CTN codons code for Thr in this genetic code, but CodonW specifies CTN as stop codons. In any case, leaving out the other 10 genetic codes severely limits the utility of  $N_c$ , especially for evolutionary biologists who are particularly interested in odd creatures that tend to feature one of those rare genetic codes. The implementation of the new  $N_c$  function in the most recent version of DAMBE (version 5.3.00) accommodates all known genetic codes.

The other problem, which is partially in concept and partially in implementation, involves the compound codon families of which there are two kinds. The first is often referred to as the 6-fold codon families each being composed of a 2-fold codon family and a 4-fold codon family, for example, those encoding amino acids Arg, Leu, and Ser in the standard genetic code. The second kind contains eight synonymous codons made of two 4-fold codon families. For example, amino acid Ser in the alternative flatworm mitochondrial code (transl\_table = 14) has eight synonymous codons that belong to two synonymous codon families, that is, TCN and AGN codon families (where N stands for any nucleotide). This genetic code was first reported (Bessho et al. 1992) after the original formulation of  $N_c$  by Wright (1990). The existence of this particular genetic code was disputed before (Telford et al. 2000) but was subsequently verified in at least two nematode species (Jacob et al. 2009).

The two codon families within each compound codon family are translated by different tRNAs and consequently could be under quite different selection pressure. Take, for example, the Leu codons in Escherichia coli 536. The 4-fold CUN codon family is translated by tRNAs from five genes, one with a G at the first anticodon site to translate Y-ending codons (where Y stands for C or U) and four with a C at the first anticodon site to translate the CUG codon, with no tRNA that forms Watson-Crick base pair with the CUA codon. This leads to a dramatic underuse of the CUA codon and over-representation of the CUG codon relative to other synonymous codons in the E. coli 536 genome. In contrast to the strong codon usage bias in the 4-fold Leu (CUN) codon family, there is no codon usage bias in the 2-fold UUR codon family (where R stands for A or G). This 2-fold codon family is translated by tRNAs encoded by two tRNA genes in the E. coli 536 genome, one with a C at the first anticodon site to translate the UUG codon and the other with a U at the first anticodon position to translate the UUA codon. This implies little selection in favor of one codon

**Table 1.** Pearson Correlation Coefficient (r) between Codon Adaptation Index and the Two Versions of  $N_c$ : the New  $N_c$  Developed in This Article and Implemented in DAMBE ( $N_{cNew}$ ) and  $N_c$  from CodonW ( $N_{c,Old}$ ).

Species	GC% <sup>a</sup>	Ngene <sup>b</sup>	Ref.File <sup>c</sup>	r (N <sub>c.New</sub> )	r (N <sub>c.Old</sub> )	T <sup>d</sup>	P <sup>d</sup>
Escherichia coli	50.80/51.82/55.88	4,254/4,233	Eeco_h	-0.7743	-0.7382	3.884	<0.0001
Bacillus subtilis	43.50/44.23/44.53	4,176/4,141	Ebsu_h	-0.5807	-0.4737	-6.766	<0.0001
Micrococcus luteus	73.00/73.16/95.14	2,236/2,235	rib. prot.	-0.7853	-0.7331	-4.127	<0.0001
Mycoplasma genitalium	31.69/31.55/23.04	475/473	rib. prot.	-0.7629	-0.7173	-1.551	0.1209
Saccharomyces cerevisiae	38.30/39.63/37.95	5,863/5,834	Eysc_h	-0.8738	-0.8444	-6.078	<0.0001
Drosophila melanogaster	42.40/53.80/63.80	22,102/22,075	Edro_h	-0.8613	-0.8318	-10.947	<0.0001
Caenorhabditis elegans	35.40/42.97/39.66	23,894/23,829	Ecel	-0.6736	-0.6430	-5.908	<0.0001

NOTE.—All correlations have P < 0.0001. The differences between each pair of r ( $N_{c,New}$ ) and r ( $N_{c,old}$ ) are highly significant (P < 0.0001) except for Myc. genitalium, which has relatively few genes. Overall, r ( $N_{c,New}$ ) is significantly greater than r ( $N_{c,Old}$ ) based on a paired-sample t-test on the seven pairs of r values (t = 4.4926, DF = 6, P = 0.0041, two-tailed test).

<sup>a</sup>Genomic GC%/coding sequence GC%/third codon position GC%.

<sup>b</sup>In format A/B where A is the total number of coding sequences (CDSs) and B is the number of CDSs after excluding those that CodonW cannot compute  $N_c$  from. GenBank accession numbers are S. *cerevisiae* (NC\_001133 to NC\_001148), E. coli (NC\_010473), B. subtilis (NC\_000964), D. melanogaster (NC\_004353, NC\_004354, NT\_033777 to NT\_033779, and NT\_037436), and C. elegans (NC\_003279 to NC\_003284).

<sup>c</sup>Name of file containing known highly expressed genes distributed with EMBOSS (Rice et al. 2000). For *M. luteus* and *Myc. genitalium*, codon frequencies from ribosomal proteins are used.

 $^{d}T$  and P values based on the test in Box 15.3 in Sokal and Rohlf (2012). All tests are two tailed.

against the other, and the two codons are used almost exactly equally in coding sequences of *E. coli* 536.

Given that the two synonymous codon families within each compound codon family are subject to quite different selection pressure for codon usage bias and often exhibit dramatically different codon usage bias (e.g., strong bias in the CUN codon family but no bias in the UUR codon family in *E. coli* 536), it makes little sense to lump them together in computing a single  $F_{CF}$ . Unfortunately, the original formulation of  $N_c$  (Wright 1990), as well as all subsequent implementations including the most widely used CodonW, did not separate the 6-fold or the 8-fold compound codon family into two separate codon families, but instead all lump the two codon families together into a single compound codon family and compute a single  $F_{CF}$ .

The implementation of the new  $N_c$  in DAMBE is the first to separate each 6-fold compound codon family into separate 2-fold and 4-fold codon families, and each 8-fold compound codon family into two separate 4-fold codon families. Treated in this way, the number of codon families is increased from 20 to 23 in the standard genetic code. With the extreme codon usage bias, that is, only one synonymous codon is used in each codon family,  $N_c$  will reach its minimum of 23.

#### Evaluation of $N_c$

The value of any new bioinformatic tools ultimately depends on whether they can solve biological problems better than existing ones. We will evaluate the new  $N_c$  in two ways. First, given the empirical results that CAI is the best predictor of gene expression at both mRNA and protein level (Comeron and Aguade 1998; Coghlan and Wolfe 2000), we will examine whether the new  $N_c$  correlates better with CAI than the original  $N_c$  (e.g.,  $N_c$  computed by CodonW). Second, we will check whether the new  $N_c$  can predict protein production better than the original  $N_c$ .

# New $N_c$ Correlates Better with CAI Than the Original $N_c$

We retrieved protein-coding sequences from three eukaryotic species (*Saccharomyces cerevisiae, Drosophila melanogaster,* and *Caenorhabditis elegans*) and four prokaryotic species (*E. coli* representing the Gram-negative bacteria, *B. subtilis* representing the Gram-positive bacteria, *Micrococcus luteus* representing GC-rich bacteria, and *Mycoplasma geni-talium* representing AT-rich bacteria). These seven species all have well-annotated genomes, and the first five also have a set of known highly expressed genes needed to compute CAI ("Ref.File" in table 1). For the last two species, the ribosomal proteins, which are typically highly expressed, are used as the set of highly expressed genes for computing CAI by the improved CAI implementation in DAMBE (Xia 2007).

The new  $N_c$  was computed by using DAMBE (with all default options that represent the method presented in this article) and the original  $N_c$  by using CodonW. CodonW cannot compute  $N_c$  for a few short genes that miss 2-fold or 4-fold codon families. These genes were excluded in computing the new  $N_c$  by DAMBE as well to facilitate a fair comparison.

The new  $N_c$  consistently exhibits stronger correlation with CAI than the original one computed by CodonW for all seven genomes, with the difference being highly significant (P < 0.0001) for six genomes (table 1), except for *Myc. genitalium* that has fewer genes and consequently a reduced power to detect the difference. A paired-sample *t*-test shows that the difference is highly significant (T = 4.4926, DF = 6, P = 0.0041, two-tailed test). This is not surprising because the advantage of our proposed modifications seem obvious.

The new  $N_c$  helps reveal patterns that would be hidden with the old  $N_c$ . Three genes (*yagF*, *yagG*, and *yagH*) from the defective CP 4–6 prophage of *E. coli* (Wang et al. 2010) have



**FIG. 1.** The new  $N_c$  facilitates the detection of newly "immigrant" genes that exhibit codon usage bias different from the "native" genes. (*a*) Three genes (*yagF*, *yagG*, and *yagH*) from the defective CP 4–6 prophage of *Escherichia coli* (Wang et al. 2010) have strongly biased codon usage (relatively small  $N_c$ ) but relatively poor codon adaptation (mediocre CAI values). (*b*) The distinction of the three genes is lost in the plot when the old  $N_c$  (computed from CodonW) is used.

strongly biased codon usage, resulting in relatively small  $N_c$  values. However, their codon usage bias is not concordant with that in highly expressed E. coli genes, resulting in relatively small CAI values. This codon usage pattern sets the three genes apart from the rest of E. coli genes (fig. 1a), which highlight the value of using the " $N_c$  versus CAI" plot to detect recently horizontally transferred genes when the source genome and the target genomes have undergone codon adaptation in different directions. Interestingly, the separation of the three prophage genes from the rest of the E. coli genes is obscured when  $N_c$  is computed from CodonW (fig. 1b). The largest mucin gene (mucin 14 A) in D. melanogaster also exhibits strong codon usage bias  $(N_c = 38.6)$  but in the direction opposite to those highly expressed D. melanogaster genes, with a CAI value equal to 0.1277, which is the second smallest among all D. melanogaster genes.

# The New $N_c$ Predicts Protein Production Better Than the Original $N_c$

For checking whether the new  $N_c$  can predict protein production better than the original one, we used the experimentally quantified protein production in the yeast, *S. cerevisiae* (Ghaemmaghami et al. 2003). This data set, with protein abundance data for 3,850 yeast genes after excluding 18 genes that do not have a matched name in the current yeast database, can be found in the online supplemental file GhaemmaghamiProtein.xls in a previous study (Xia et al. 2011). After excluding genes that miss 2-fold or 4-fold codon families, 3,839 genes remain, and their log-transformed values (In Prot) were correlated to CAI, the new  $N_c$  computed from DAMBE, and the original  $N_c$  from CodonW.

The new  $N_c$  correlates better with ln Prot than the original  $N_o$  with Pearson correlation being -0.5739 between the new  $N_c$  and ln Prot and -0.5412 between the old  $N_c$  and ln Prot. The two Pearson correlation coefficients are significantly different (z = -2.093, P = 0.0364) according to the test detailed in Sokal and Rohlf (2012, pp. 573–575).

The correlation between CAI and ln Prot is 0.5981. It is highly significantly stronger than that between the old  $N_c$  and ln Prot (z = 3.722, P = 0.0002) but not significantly stronger than that between the new  $N_c$  and ln Prot (z = 1.629, P = 0.1033)

In summary, the new  $N_c$  offers four key advantages over the original  $N_c$ : 1) the minimum and maximum will now be the number of codon families and the number of sense codons, respectively, 2) biases associated with codon families with a small number of codons are alleviated by pseudocounts and by weighting, 3) compound codon families are properly handled by separating them into individual codon families, and 4) all known genetic codes are accommodated. It consistently correlates better with CAI and can predict protein production better than the original  $N_c$ .

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